POTENTIAL ENERGY SURFACE OF $[Cu(H_2O)_6]^{2+}$ AND $[Zn(H_2O)_6]^{2+}$ DERIVED FROM AB INITIO MO CALCULATIONS

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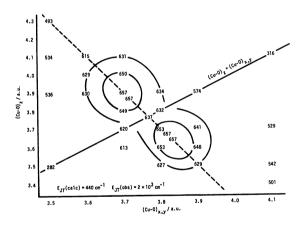
Ab initio molecular orbital calculations on $[{\rm Cu(H_2O)}_6]^{2+}$ and $[{\rm Zn(H_2O)}_6]^{2+}$ have been carried out to obtain the metal-oxygen bond lengths. The calculated results are in qualitative agreement with the expectation from the Jahn-Teller theorem; a distorted octahedron for ${\rm Cu}^{2+}$ and a regular octahedron for ${\rm Zn}^{2+}$. However, the preference for an elongated octahedron observed in the ${\rm Cu}^{2+}$ complex was not shown by the present calculation.

Six-coordinate copper(Π) complex is known to take distorted octahedral shapes, in accordance with the Jahn-Teller theorem. Experimental evidence has been gathered by Reinen et al. for the perference of elongation along the tetragonal axis. Recently, Yamatera has shown that configuration interactions would probably stabilize the $^2B_{1g}$ ground state of the elongated octahedral complex to a greater extent than the $^2A_{1g}$ ground state of the compressed octahedral complex and that the $^4B_{1g}$ ground state of the compressed octahedral complex and that the $^4S_{1g}$ mixing would make a significant contribution to the energy difference between the $^2B_{1g}$ and $^2A_{1g}$ states. With an intention to obtain a deeper understanding of the stereochemistry of copper(Π) complexes, we have performed ab initio molecular orbital calculations on the $[Cu(H_2O)_6]^{2^+}$ ion, which is real, easy to be calculated, and of interest in solution chemistry. Calculations were also made on $[Zn(H_2O)_6]^{2^+}$ for comparison. The structures of these ions in solution have been determined using the X-ray diffraction by Ohtaki et al. and EXAFS by Sano et al. as follows: $(Cu-O)_{\pi} = 2.43 \text{ Å} (4.595 \text{ a.u.})$ and $(Cu-O)_{\pi} = 1.94 \text{ Å} (3.667 \text{ a.u.})$, and $(Zn-O)_{\pi} = 2.43 \text{ Å} (4.595 \text{ a.u.})$.

The calculation was done in the SCF LCAO MO scheme with the basis set of Gaussian functions by using a program package JAMOL3 written by Kashiwagi et al. $^{6)}$ The single-zeta basis sets are $[10s,6p,3d/4s,3p,1d]^{7)}$ for Cu and Zn, [7s,3p/2s,1p] for O, and [3s/1s] for H, respectively. $^{8)}$ The ion was assumed to be D_{2d} symmetry and the interatomic distance between O and H was taken as 1.0 Å and the HOH bond angle 106.4° . The D_{2d} symmetry, which is D_{4h} minus the center of symmetry, is practically equivalent to D_{4h} in the present calculations which are concerned with gerade electronic states. Thirty and seventeen calculations, respectively, for the Cu and Zn complexes have been done with axial and equatorial metal-oxygen bond distances as variables. Figures 1 and 2 show the calculated potential energy surfaces for $[Cu(H_2O)_6]^{2+}$ and $[Zn(H_2O)_6]^{2+}$ ions, respectively. The error in the calculation of the total energies is less than 1×10^{-4} a.u. The digits given in

Figs. 1 and 2 are the last three significant figures of the total energy values, -2086.4 and -2224.7 a.u. for the Cu and Zn complexes, respectively. A regular octahedron is stable for $[Zn(H_2O)_6]^{2+}$, and the calculated Zn-O bond length is 3.78 a.u. in agreement with the result of Clementi et al. $(3.74 \, a.u.)^9)$ and slightly less than the experimental value (3.932 a.u.). 4) On the other hand, [Cu(H₂O)₆]²⁺ showed two minima of the energy at the (Cu-O)₂ and (Cu-O)₃ bond lengths of 3.90(z) and 3.70(x,y) and of 3.667(z) and 3.817(x,y) a.u. No significant difference in energy was found between the two minima. The experimental bond lenghts⁴⁾ are 4.595(z) and 3.667(x,y), and their ratio is 1.25 which is much greater than the calculated value of 1.05. The calculated Jahn-Teller energy was $440~{
m cm}^{-1}$ which is about 1/5 of the experimental value. The smaller extent of Jahn-Teller distortion derived from the calculation may result from: (1) the neglect of solvent effect, (2) the limited basis set, and (3) the restricted Hartree-Fock formalism without configuration interactions. Additional calculations as described below did not affect the conclusion.

Calculations on the $(H_2O)_6$ cluster with the geometries of the stable $[Cu(H_2O)_6]^{2+}$ forms gave the total energies of -454.0149 (elongated) and -454.0149 a.u. (compressed), showing that the energies of ligand-ligand interactions are nearly identical in the two forms. Calculations were also made using a basis set with split d-functions; no significant difference in the total energy was found between the elongated and compressed complexes.



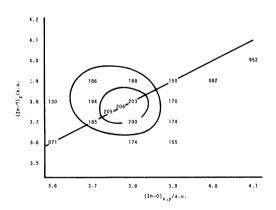


Fig. 1 $[Cu(H_2O)_6]^{2+}$ Potential Surface

[Zn(H₂O)₆]²⁺ Potential Surface Fig. 2

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